Non-Statistical Sampling
Purpose

The purpose of this booklet is to inform taxpayers, practitioners, and other interested parties of the sampling methods that can be used by the Department and to provide a general understanding of what to expect if the auditor uses non-statistical sampling. Although the emphasis is upon sales and use tax, the same procedures may be used for audits of other taxes administered by the Florida Department of Revenue.

Credits

Designed and developed by the Florida Department of Revenue, General Tax Administration Statistics Team.

Sponsored by:

State of Florida
Department of Revenue
General Tax Administration Program
Compliance Review Process
Tallahassee, Florida
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<tr>
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</tbody>
</table>
Non-Statistical Sampling

The nature of your records will determine the best audit plan for your business. The most accurate and unbiased audit is a detail audit, where each record in the audit period is examined to determine the actual amount of additional tax due or overpaid. A detail audit may be required by statute for some record types. Generally, the amount of time needed to complete a detail audit is exorbitant, unless the records are available electronically.

When auditing a taxpayer with voluminous records, sampling usually reduces audit time, thereby increasing efficiency and reducing costs for the Department and taxpayers. Sampling is the procedure of taking a small sample from a much larger population and making inferences from the sample about the population.

Sampling techniques can be statistical or non-statistical. A statistical sample requires random selection of sample points and statistical evaluation of the sample results by measuring precision. (See Form GT-300034, Auditing in an Electronic Environment, for more information on stratified statistical sampling.) Non-statistical sampling techniques may randomly or judgmentally select sample points, but do not statistically evaluate sample results. This booklet covers non-statistical sampling using random selection.

<table>
<thead>
<tr>
<th>Statistical</th>
<th>Non-Statistical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Randomly selected sample points. Auditor and taxpayer have no control over selection. Sample selection is objective.</td>
<td>Randomly selected sample points. Auditor and taxpayer have no control over selection. Sample selection is objective.</td>
</tr>
<tr>
<td>Statistical sampling has an objective way of measuring sampling error (precision).</td>
<td>No way of measuring the precision.</td>
</tr>
</tbody>
</table>

**Comparison of Sampling Techniques**

**Legal Authority**

Under Florida Statutes, any taxpayer conducting business in Florida who collects sales and use tax and files returns is required to keep records and other information that will allow the Department to determine the correct amount of tax due. Section 212.12(6)(c), Florida Statutes, provides that the Department may sample a taxpayer’s records, except fixed assets, when the records are adequate and voluminous. When records are adequate and voluminous for the entire audit period, overpayments found in the sample may be projected over the entire audit period. The requirements for a refund or credit must be met for an overpayment to occur.
According to s. 212.12(6)(b), F.S., if a taxpayer does not have adequate records of retail sales or purchases, the Department may project a deficiency from a sample of the taxpayer’s available records. There is no provision in (6)(b) to project an overpayment for taxpayers who do not have adequate records. When a taxpayer’s records are inadequate, any refund or credit must be verified by a detail examination of the records available concerning the refund. The auditor must document in the case file the nature of the taxpayers’ records and the basis for his or her determination.
Selecting the Sample

The first step in selecting the sample is to identify the sampling frame. The sampling frame is a group of items from which the sample is drawn or a listing of sampling units. In a homogeneous sampling frame, any item in the frame is representative of any other item; therefore, a random selection of all items in the frame will be representative.

The auditor determines how the accounting records are physically stored and available in order to identify the sampling frame. Typically, accounting records have numbered sampling frames or non-numbered sampling frames, or they may have a combination of both.

Both numbered and non-numbered sampling frames can be randomly sampled using WinSample. WinSample is a software program developed by the General Tax Administration’s Statistics Team and Applied Technology. WinSample randomly selects sample points from many possible sampling frames using a seed number. WinSample may be used when taxpayer records are not available in an electronic format suitable for stratified statistical sampling or e-Auditing.

Numbered sampling frames include source documents that are consecutively numbered. Some examples are:

- Invoice numbers
- Voucher numbers
- Check numbers

Non-numbered sampling frames include source documents that have no natural numbering system. Although not consecutively numbered, a random sample of the transactions may still be identified. Some examples of non-numbered sampling frames supported in WinSample are:

- Time periods (days, weeks, months, quarters)
- Journals (with page numbers and multiple lines on each page)
- Imaged documents
- Microfiche

After the sampling frame is identified, data integrity tests for each sampling frame should be performed. Data integrity tests should be performed on both numbered and non-numbered populations. Acceptance sampling can be used in tax auditing to assist in determining data integrity and whether a taxpayer’s records are adequate or inadequate.
Non-Statistical Sampling

Acceptance sampling is a statistical sampling technique used to obtain information for the purpose of estimating whether an event has occurred and the total number of times it occurred. The acceptance number is the maximum number of transactions that can fail the data integrity test at the selected sample size. There are three ways that any sample point can fail the data integrity test:

- Sample point is physically missing.
- Sample point is not recorded in the accounting records.
- Sample point is incorrectly recorded in the accounting records (tax amount or total amount is wrong, or the sample point is misclassified).

The table below shows minimum sample sizes for each acceptance number at a 95% confidence level. For further discussion and statistical basis for acceptance sampling, see Appendix 6.

<table>
<thead>
<tr>
<th>Minimum Sample Size</th>
<th>Acceptance Number</th>
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<tbody>
<tr>
<td>100</td>
<td>1</td>
</tr>
<tr>
<td>150</td>
<td>3</td>
</tr>
<tr>
<td>180</td>
<td>4</td>
</tr>
<tr>
<td>200</td>
<td>4</td>
</tr>
<tr>
<td>220</td>
<td>5</td>
</tr>
<tr>
<td>240</td>
<td>6</td>
</tr>
<tr>
<td>260</td>
<td>6</td>
</tr>
<tr>
<td>300</td>
<td>7</td>
</tr>
<tr>
<td>320</td>
<td>9</td>
</tr>
<tr>
<td>340</td>
<td>10</td>
</tr>
<tr>
<td>360</td>
<td>11</td>
</tr>
<tr>
<td>380</td>
<td>12</td>
</tr>
<tr>
<td>400</td>
<td>13</td>
</tr>
</tbody>
</table>

If the accounting records fail the data integrity test, the following situations apply:

- Credits resulting from the sample cannot be projected.
- Accounting totals and reports may not be reliable.
- Penalty reduction may not be recommended.

Once data integrity tests are performed, the sample is selected using WinSample. Spares may also be selected as well. Spares are extra sample points used to replace either non-existent sample points or non-transactions.
Suggested sample sizes can be based on the following guidelines:

- Acceptance sampling
- Central limit theorem
- Student’s t
- Taxpayer request

The sample points selected for acceptance sampling can also be used as the sample points to determine compliance. Whether the records are adequate or inadequate, the randomly selected sample points can be used for the sample.

The central limit theorem applies when a sample size of at least 30 sample points is used. In accordance with the central limit theorem, the sample means will be normally distributed for random samples taken from the population, regardless of the population’s distribution or size. Therefore, a sample of 30 sample points can be used if this method is selected. See the Appendices for the normal distribution table.

The student’s t distribution can be used for sample sizes less than 30 sample points. Based on statistical methodologies, a minimum sample size of 5 is recommended. Further discussion of the student’s t distribution is found in the Appendices.

A sample size may be requested by the taxpayer. The auditor’s experience and judgment as well as the suggested sample size guidelines will be used to determine if the taxpayer’s requested sample size is large enough.

Suggested sample sizes listed below are based on acceptance sampling, the central limit theorem, or student’s t distribution for each sampling frame.

<table>
<thead>
<tr>
<th>Sampling Frame</th>
<th>Suggested Sample size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Numbered</td>
<td>Acceptance sampling # or 30 sample points</td>
</tr>
<tr>
<td>Non-Numbered:</td>
<td></td>
</tr>
<tr>
<td>• Time Periods (Days)</td>
<td>5 or 30 days</td>
</tr>
<tr>
<td>• Time Periods (Weeks)</td>
<td>5 weeks</td>
</tr>
<tr>
<td>• Time Periods (Months)</td>
<td>5 months</td>
</tr>
<tr>
<td>• Time Periods (Quarters)</td>
<td>2 quarters</td>
</tr>
<tr>
<td>• Journal Pages and Lines</td>
<td>Acceptance sampling # or 30 sample points</td>
</tr>
<tr>
<td>• Image Documents</td>
<td>Acceptance sampling # or 30 sample points</td>
</tr>
<tr>
<td>• Microfiche Documents</td>
<td>Acceptance sampling # or 30 sample points</td>
</tr>
</tbody>
</table>
Completing the Sample

The Department requests source documents to verify the tax treatment of the sample points. If tax was due on a transaction and not paid or accrued, an underpayment is scheduled in the audit workpapers. If tax was not due on a transaction, but paid or accrued in error, an overpayment will be scheduled in the audit workpapers if the taxpayer has met the requirements for a refund of taxes paid to the Department in error. All sample points will be examined and documented in the audit workpapers. Correctly taxed transactions will not be deleted, but will hold 0.00 additional tax due value.

Negative invoices are entered as credit amounts. This does reduce the sample base; however, negative sample points (i.e. credit memos) normally occur in any population. Gross sales and other population totals include negative amounts, and they are not adjusted.

Outliers are items that are larger or smaller than the majority of items in the population. They are also called extraordinary, exceptional, or non-recurring items. Any random sample may contain what others may consider outliers. With simple random sampling, all items in the population have an equal chance of being selected. You should not remove any sample points from your sample. All sample points are projected.

The results of the sample are provided to the taxpayer during the audit, so that any available supporting documentation can be located. Any sample points without supporting source documents are considered taxable and will be scheduled as an underpayment.

Non-existent or non-transaction sample points will be replaced by spare sample points in the order selected by the WinSample program. Examples of non-existent or non-transactions for each type of sampling frame include:

Numbered Sampling Frames
- Voided invoices.
- Voided checks.
- Voided vouchers.
- Fixed asset invoices are examined in detail by statute.
- Real property rental or other transactions are easily examined in detail.
- Transactions outside the audit period.

Non-Numbered Sampling Frames
- Time periods – days, months, weeks or quarters where the business was closed (holidays, etc.).
- Journal pages or lines that do not exist.
- Image frame that does not exist.
- Image frame that does not contain an invoice (envelopes, correspondence, etc.).
- Microfiche row or column that does not exist on the selected sheet.
- Transactions outside the audit period.

Non-statistical sampling does not calculate precision and there is no statistical evaluation of the sample results, so expanding the sample is a judgmental decision made by the auditor, the auditor’s manager, and/or the taxpayer.
If the sample is expanded, any remaining spares will be examined in the order selected. If necessary, additional sample points will be randomly selected from the original sampling frame using WinSample and the same seed number used to select the original sample points. The additional sample points are then added to the original sample transactions in the exhibit and audited for tax compliance.

**Projecting and Allocating Sample Results**

The ratio estimator is the preferred estimator for non-statistical sampling because it weighs any errors of the sample proportionately by dollar value. The difference estimator is an average error per sample point. With non-statistical sampling, the difference estimator may skew the average because of the increased variability of the sample without stratification.

The ratio estimator calculates a percentage based on the ratio of the sample results to the sample base. In the case of overpayments, the sample results would be a negative amount divided by the sample base. The ratio is multiplied by the sampling frame dollars per month to obtain total additional tax due or overpaid for the exhibit.

The sample results may be represented by additional tax due or additional taxable amount. If additional tax due is used the ratio is called the percentage of error. If additional taxable amount is used the ratio is called the error ratio.

The percent of error exhibit calculates a percentage of the total additional tax due of the sample points divided by the sample base:

\[
\frac{\text{Additional tax of the sample points}}{\text{Sample base}}
\]

The percent of error is multiplied by the total value of the sampling frame to obtain additional tax due or overpaid for the population. The percent of error can be used when sales are made to multiple counties with varying tax rates or purchases are acquired in multiple counties. Separate exhibits for each county may also be used in audits with multiple counties.

The error ratio exhibit type calculates a percentage of the total additional taxable amount of the sample points divided by the sample base:

\[
\frac{\text{Additional taxable amount of the sample points}}{\text{Sample base}}
\]
Non-Statistical Sampling

The error ratio is multiplied by the total value of the sampling frame to obtain additional taxable amounts for both the state and county for the exhibit. The error ratio should only be used when sampling just one county since the additional taxable amount is multiplied by the state and county rate for each month in the period.
Appendix 1  

Sampling Survey

The answers to the following questions will help determine appropriate sampling frames for each audit:

1. How many sales invoices are generated per month?
2. How many purchase invoices are paid each month?
3. Are any of the source documents numbered sequentially? Are they filed that way?
4. How and where are the source documents physically filed?
5. Are source documents available on journals, microfiche, or imaging systems?
6. If there is an imaging system, which documents are imaged? (Invoices, purchase orders, correspondence, envelopes, interoffice memos, etc.)
7. Are there any source documents not available for review?
8. Have the operations of the company significantly changed during the audit period? (Changes in accounting staff, computer system, operations, etc.)
9. Does the company separate sales and/or purchases transactions by location, product line, or in some other manner (by department, store location, division, etc.)?
10. Are fixed asset transactions filed separately from general purchases?
11. Are sales invoices for Florida sales and out-of-state sales filed together?
12. Are sales invoices for both exempt and taxable sales filed together?
13. Are inventory purchases (for resale) filed separately from general expenses?
14. When are the DR-15s filed, i.e., monthly, quarterly, semi-annually, or annually?
15. How are the DR-15s filled out – are all sales combined or are they separated?
16. If the DR-15s contain combined sales figures, are monthly totals for each area to be sampled available?
17. What is the fiscal year of the company?

18. Are there any days when the company is closed?

19. If records are filed weekly, what constitutes a week? (Mon. – Fri., Tue. – Sat., etc.)

20. If records are filed quarterly, what constitutes a quarter? (Jan. – Mar., Feb. – Apr., etc.)
## Appendix 2  Non-Statistical Sampling Steps

### Selecting the Sample

<table>
<thead>
<tr>
<th>Step</th>
<th>Action</th>
<th>Considerations</th>
<th>Result</th>
</tr>
</thead>
</table>
| 1    | Identify the sampling frame.               | • Numbered records: Single range, multiple ranges, either overlapping or non-overlapping.  
• Non-numbered records: Time periods (days, weeks, months, quarters), journals, imaged documents, or microfiche. | The most homogeneous sampling frame is determined, based on how the taxpayer records and stores its records. |
| 2    | Select a sample size.                      | • Acceptance sampling  
• Central limit theorem  
• Student’s t  
• Taxpayer request | A sample size is selected.                                                   |
| 3    | Randomly select sample points.             | • Select the appropriate option in WinSample.  
• Set sampling frame parameters.                                              | A randomly selected sample is generated using WinSample.                |
### Completing the Sample

<table>
<thead>
<tr>
<th>Step</th>
<th>Action</th>
<th>Considerations</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Audit the sample points.</td>
<td>• Create exhibits in Department software.</td>
<td>The sample will be examined and the results recorded in Department software.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Examine documentation.</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Record results in Department software.</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Replace sample points, if needed, with spares.</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>Expand the sample.</td>
<td>• Review sample results with taxpayer.</td>
<td>The sample will be expanded to include additional sample points.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Determine whether to expand the sample.</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Examine remaining spares.</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Select additional sample points using WinSample.</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>Review additional sample points.</td>
<td>• Import additional points into Department software.</td>
<td>The expanded sample is audited.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Review additional documentation.</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Record results.</td>
<td></td>
</tr>
</tbody>
</table>

### Projecting and Allocating Sample Results

<table>
<thead>
<tr>
<th>Step</th>
<th>Action</th>
<th>Considerations</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>Project sample results.</td>
<td>• Import or enter the monthly amounts to use for projecting sample results.</td>
<td>Sample results are projected to the sampling frame.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Prepare % of error or error ratio schedule.</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>• Prepare additional tax due schedule.</td>
<td></td>
</tr>
</tbody>
</table>
Appendix 3  

Sampling Agreement

This agreement made and entered into by and between the Florida Department of Revenue, hereafter referred to as “The Department,” and Company Name, FEI# ___________, Audit #_________________, hereafter referred to as “Taxpayer.” The Department and Taxpayer will be collectively referred to herein as “Parties.”

WITNESSETH

WHEREAS, the Parties wish to facilitate the completion of a sales and use tax compliance audit, Audit Number ________________;

WHEREAS, the Parties agree that the records of Taxpayer are so voluminous in nature and substance that a sampling is an effective, expedient, and adequate method to facilitate the audit;

NOW, THEREFORE, in consideration of the mutual premises contained herein, it is hereby agreed to by the Parties as follows:

1. Pursuant to section 212.12(6) (c), Florida Statutes, the audit of Taxpayer for the period __________ shall be controlled by the sampling method set forth in the sampling plan(s) included in the audit workpapers.

2. This sample shall be deemed to be representative of all of the transactions pertaining to Taxpayer’s business and the findings of this sampling shall be projected over the period set forth in the sampling plan(s).
In Witness whereof, we as representatives of the respective parties have hereunto set our hand and in so doing we hereby bind the parties who we represent.

FLORIDA DEPARTMENT OF REVENUE

By:____________________________________

Jim Zingale, Executive Director or his designee(s)

Title Date

By:____________________________________

Officer or owner of business

Title Date
Appendix 4  
Sampling Plan

This sampling plan explains and defines the sampling method to be used in conducting the sample of sales invoices.

<table>
<thead>
<tr>
<th>TAXPAYER NAME</th>
<th>AUDIT NO. <strong>0201234577</strong>_________</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sample Company</td>
<td>FEI# ____________________________</td>
</tr>
</tbody>
</table>

1. Define the Sampling Frame

Florida Department of Revenue auditors will sample sales invoices from the period 01/01/2000 – 12/31/2002. Sales invoices are consecutively numbered beginning with invoice #10000 and ending with invoice #18000 for the audit period, which will be the sampling frame.

2. Method of Sampling

The method used for sample selection will be simple random sampling. Spare sample points will be identified in the event that an invoice selected is non-existent or a non-transaction (voided invoice, an invoice never issued, etc.).

3. Sample

A sample of 100 sample points will be examined and the results used to determine tax compliance. A total of 25 spares will be identified and used for non-existent or non-transactions. If needed, spares will be used in the order selected.

4. Random Selection of Sample Points

The sample has been randomly selected from the population using Department software (WinSample) and the randomly generated seed number (see below). Taxpayer will provide the Department with the source documents for the sample points selected. The auditor will determine additional tax due or overpaid for each sample point. The auditor will review and discuss the results of the sample with the taxpayer. If requested, the sample may be expanded to include additional sample points. Additional sample points, if needed, will be selected using the same seed number below.

Random Selection Seed Number: 23242012
5. Calculation of Additional Tax Due or Overpaid

Additional tax due or overpaid will be calculated using the ratio estimator. The ratio estimator calculates a percentage of error based on ratio of additional tax due or overpaid from the sample divided by the dollars examined in the sample.

The auditor will schedule all sample points into the exhibit to determine the sample base for the sampling frame. Exceptions will be totaled and a percentage of error will be calculated. This percentage will then be multiplied by sampling frame totals, which are the monthly amounts of the sales invoices as reported on taxpayer’s financial statements. The Sales and Use Tax Returns (DR15s will not be used for projecting the error, since the sampling frame includes only sales invoices, and the gross sales reported on the DR-15s include other sales that were not sampled.

There is no minimum number of errors. If no errors are found, additional tax due or overpaid is 0.00 for the exhibit. Even if only a single error is found, it is projected, whether the error is a tax deficiency or overpayment.

6. Sampling Plan Applicable Only to the Taxpayer

This sampling plan is only applicable to the Taxpayer identified above and is not intended to be a rule or a statement of general applicability.
### Appendix 5  
**Acceptance Sampling Table**

**ACCEPTANCE SAMPLING (HYPERGEOMETRIC PROBABILITIES)**  
**SAMPLE SIZES AND ACCEPTANCE NUMBERS**  
**PROBABILITY THAT ERROR IN A UNIVERSE > 1000 IS < :**

<table>
<thead>
<tr>
<th>Sample Size Examed</th>
<th>No. of Errors Found</th>
<th>5%</th>
<th>Sample Size Examed</th>
<th>No. of Errors Found</th>
<th>5%</th>
</tr>
</thead>
<tbody>
<tr>
<td>40</td>
<td>0</td>
<td>87.15</td>
<td>260</td>
<td>0</td>
<td>100.0</td>
</tr>
<tr>
<td></td>
<td>1</td>
<td>60.10</td>
<td></td>
<td>1</td>
<td>100.0</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>92.31</td>
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<td>2</td>
<td>99.91</td>
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<td></td>
<td>3</td>
<td>72.06</td>
<td></td>
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Appendix 6        Acceptance Sampling

Attributes Sampling Plans AKA Acceptance Sampling
Attribute Sampling Plans
©Dr. C. G. Chentnik
December 2, 2002

These plans are used to estimate the rate (percentage) of occurrence of a specific quality (attribute) in a population. They answer the question: “How Many?” We might use this type of sampling plan to estimate the number of taxable invoices. A possible conclusion using attributes sampling could be that “There is only a 5% risk that the true rate of taxable entries in our population exceeds 6%.”

Any statistical sampling plan will by its very nature have inherent estimation errors. The suggestion is to detail or look at every data point rather than sample. The decision to sample the taxpayer’s records is a managerial one based on the cost of detailing each and every record. Any detail sample will be more accurate than one involving a prediction based on statistics. We use statistics to estimate the parameters of interest. It is my recommendation to detail as large a population as is cost effective before resorting to a sampling methodology.

Notation -- Acceptance Sampling

R = number of successes or complete record matches

n = number of trials

π = trial success probability

r = 0, 1, 2, 3, ... , n

n = sample size for our problem

P= the Population proportion of correct records

Q= (1-P) or the Population proportion of incorrect records

p= the sample proportion of correct records

q= (1-p) or the sample proportion of incorrect records
\[ \sigma_p = \sqrt{\frac{PQ}{n}} \]

= it is assumed that \( p \) is normally distributed about \( P \) and therefore this is an approximate statement for the standard deviation of the probability distribution of interest.

Since \( p \) is assumed normally distributed about \( P \), upon repeated sampling, it will lie within the range \( (P \pm 2\sigma_p) \) with a 95% chance. Hence, this expression is applicable:

\[
2 \sqrt{\frac{PQ}{n}} = 5 \% = 0.05 \quad \text{or} \quad n = \frac{4PQ}{0.0025}
\]

\( \forall \ p \leq 0.5, \)

\( n \leq 400. \)

Notice the difficulty that appears and is common to every problem of estimating the correct sample size. Namely an expression for \( n \) has been developed where \( n \) depends on the very property of the population we want to estimate — \( P \). We therefore need some idea of the likely value of \( P \).

\( Pr = \) a probability statement

\( d = \) actual error of estimation; some tolerable margin of error \( d \) in the estimated proportion

\( \alpha = \) the risk that we are willing to incur that the actual error is larger than \( d \)
Discussion

The extant situation is likened to a Bernoulli process, which is described as a random experiment consisting of a sequence of trials (randomly drawn sample points) which is characterized by:

1) Each sample point can have only one of two possible outcomes — success or failure. (Success in our situation is defined as a correct record match and failure is an incorrect match.)

2) Every outcome of each preceding trial’s results is independent of all other trials.

3) The probability for success is a stationary constant for all trials.

4) The probability for success is p and the probability for failure is q = (1-p) and their definitions are interchangeable.

If, as in our case, the outcomes are the results of a Bernoulli process, then the number of successes – R — is said to have a binomial distribution.

The below expression, referred to as the binomial formula, is appropriate for any Bernoulli process:

\[ Pr[R=r] = \frac{n!}{r!(n-r)!} \pi^r (1-\pi)^{n-r} \]

where, R = number of successes or complete record matches
n = number of trials
\( \pi \) = trial success probability
r = 0, 1, 2, 3, ..., n
! = Factorial

If we are interested in the proportion of successes r/n we have this probability formula:

\[ Pr[ P=r/n ] = \frac{n!}{r!(n-r)!} \pi^r (1-\pi)^{n-r} \]

Where, P = r/n is the proportion of successes.

An interesting and fundamental property of the binomial distribution is that we may approximate its probability density function with that of the normal probability function. This fundamental property holds for all values of \( \pi \) (excepting the obvious cases of 0 and 1), as n becomes large.
Cumulative probability distribution for the proportion of correct records in the taxpayer’s records:

\[
\begin{array}{cccc}
 r & r/n = r/10 & P\{ P = r/n \} & P\{ P \leq r/n \} \\
0 & 0 & .0060 & .0060 \\
1 & .1 & .0404 & .0464 \\
2 & .2 & .1209 & .1673 \\
3 & .3 & .2150 & .3823 \\
4 & .4 & .2508 & .6331 \\
5 & .5 & .2007 & .8338 \\
6 & .6 & .1114 & .9452 \\
7 & .7 & .0425 & .9877 \\
8 & .8 & .0106 & .9983 \\
9 & .9 & .0016 & .9999 \\
10 & 1.0 & .0001 & 1.000 \\
\end{array}
\]

The unit normal approximation to the binomial uses these established statistical constructs:

\[
E(P) = \pi \quad \text{or the mean or expected value E is what is used in the unit normal’s case}
\]

\[
\sigma_p = \sqrt{\frac{\pi (1-\pi)}{n}}
\]

Assuming that P has a sampling distribution that is shaped like a unit normal, we can convert P into a unit normal variable by the following transformation:

\[
Z = \frac{P - \pi}{\sigma_p}
\]

From these relationships we can proceed to use all the tools provided by the unit normal probability distribution.
Acceptance Sampling

In our problem we would be using a variant of attributes statistical sampling called acceptance sampling.

We want to accept/certify the auditee’s record keeping system as adequate or it has “data integrity” with some set minimum quality. Consider a small sample problem: the size of the records’ base submitted for approval is N=5000. The desired success rate is 95%; the sample size is n=100. The decision rule is if 7 or fewer failures (non-matches) are detected in the sample, the taxpayer’s records are accepted as meeting the minimum 5% defective criterion.

The number 7 is called the acceptance number. Thus the taxpayer’s records will be accepted if the sample proportion defective \( P \) is less than or equal to \( 0.07 = 7/100 \). Suppose that \( \pi = 0.10 \). If we knew that \( \pi = 0.10 \), the taxpayer’s records would not be accepted. We need:

\[
\sigma_p = \sqrt{\frac{0.1(1-0.1)}{100}} = 0.03
\]

The probability of acceptance therefore is computed in this fashion:

\[
P \left[ P \leq 0.07 \right] = P \left[ \frac{P - \pi}{\sigma_p} \leq \frac{0.07 - 0.10}{0.03} \right] = 1.00 = Z \text{ value}
\]

\[
P \left[ Z \leq 1.00 \right] = 0.5000 - 0.3413* = 0.1587
\]

*Read from a table of unit normal probabilities

Thus there would be a 15.87% (called the consumer’s risk) probability of accepting a record’s base which truly has a fraction defective greater than 5%. For this sampling plan to work, it is clear that either a smaller acceptance number is appropriate or a larger sample size is necessary.

If we were to lower our acceptance number to 6, we would have:

\[
P \left[ P \leq 0.06 \right] = P \left[ \frac{P - \pi}{\sigma_p} \leq \frac{0.06 - 0.10}{0.03} \right] = 1.333333
\]

\[
P \left[ Z \leq 1.333333 \right] = 0.5000 - 0.4085* = 0.0915 \quad \text{or} \quad 9.15\%
\]
If we were to lower our acceptance number to 5, we would have:

\[
P \left[ P \leq .05 \right] = P \left[ \frac{P - \pi}{\sigma_p} \leq \frac{.05 - .10}{.03} \right] = 1.666666
\]

\[
P \left[ Z \leq 1.666666 \right] = .5000 - .4525 = .0475 \quad \text{or} \quad 4.75\%
\]

This last result meets these strictest requirements, but only if we know that \( \pi \) is really = .10 .

Another kind of erroneous decision may be made. Let us suppose that the true value \( \pi \) is really .05 in the above instance. Since 8 or more defective records would give cause for rejection, a different type of mistake is committed: rejecting a good record’s base because we had a larger number of defectives show up in our sample than we can abide. We might want to know this probability — called the producer’s risk.

\[
\sigma_p = \sqrt{\frac{.05(1-.05)}{100}} = .0217944
\]

\[
P \left[ .07 > P \right] = P \left[ \frac{.07 - .05}{.0217944} \right] = .9176669
\]

\[
P \left[ .9176669 < Z \right] = .5000 - .3485 = .1515
\]

Thus there is a 15.15% chance that a good record’s base will be erroneously rejected; this is called the producer’s risk. These errors are also known as Type I and Type II errors.

Both of these latter computations revolve around the fact that we know \( \pi \). In actuality we do not know this value. We therefore would tend toward increasing the sample size until we felt at ease with these errors.

**Sample Size Determination for Acceptance Sampling**

We must determine the parameter to be estimated and the standard deviation of its point estimator. Then:

1. Solve this equation for the sample size:

2. Choose B, the bound on the acceptable margin of error, and a confidence coefficient \( (1-\alpha) \), \( Z_{\alpha/2} \times (\text{standard deviation of the estimator}) = B \) where \( Z_{\alpha/2} \) is the value of Z having area \( \alpha /2 \) to its right.

The bound B on the margin of error is .05 = 5%.
Since the confidence coefficient is $1 - \alpha = .90$, $\alpha$ must equal .10 and $\alpha/2$ is .05. The Z value from a unit normal which corresponds to a probability equal to .05 in the upper tail is $Z_{.05} = 1.645$.

Thus: $1.645 \sqrt{P(1-P)/n} = .05$  

In order to solve this equation we need a value for $p$; we use a value of .05 

Thus*** $1.645 \sqrt{.05(.95)/n} = .05$ or $n = (1.645)(.0475) = (15.6275)^2 = 244.2$ or 244. 

*** if we were to substitute $p = .5$, the largest possible solution for $n$ falls out of the equation thusly, 

$1.645 \sqrt{.5(.5)/n} = (1.645)(.5) \sqrt{n} = (16.45)^2 = 270.6$ or 271 

We have determined that even if the true value for $\pi$ lies between .05 and .5 our sample size doesn’t vary significantly; thus we would opt for the larger one. For our problem we want:

$Pr( | p - P | \geq d = \alpha$ 

We assume random sampling from a normal distribution for $p$. 

$\sigma_p = \sqrt{(N-n)/(N-1)} \sqrt{PQ/n}$ 

therefore for a particular desired degree of precision we get 

$d = z \sqrt{(N-n)/(N-1)} \sqrt{PQ/n}$ 

where $z$ is the abscissa of the normal curve that cuts off an area $\alpha$ at the tails. 

Therefore, $n = \frac{z^2PQ / d^2}{1 + 1/N \{ (z^2PQ / d^2) - 1 \}}$
An advance estimate $p$ for $P$ is usually substituted here. Also if $N$ is large the finite population correction factor (fpcf) $(N-n)/(N-1)$ reduces this expression to

$$n_o = z^2 pq / d^2 = pq / V$$

where,

$$V = pq / n_o$$

is the desired variance of the sample population

So, if: $d = 0.05$, $p=0.5$, $\alpha=0.05$, and $z=2$ we have

$$n_o = (4) (0.5) (0.5) \times 0.0025 = 400$$

This is a result where there will only be minimal increases in precision beyond this sample size. This sample size will be adjusted downward only if the fpcf is greater than 5% of the population size.

This computation of the sample size for a population size of 3,000 would be:

$$n = \frac{n_o}{1 + (n_o - 1)/N} = 400/ (1 + 399/3000) = 400 / (1 + .1330) = 353$$

In other words, a sample size greater than 400 returns only a trivial increase in sample precision and is a pseudo-maximum size for the normal approximation to the binomial distribution.

All of this development has assumed sampling without replacement. Because of this we can use the binomial distribution instead of the hyper-geometric probability density function. Whenever we have a population size of 8,000 or more, we would use 400 as a sample size. (When $400 \geq 5\%$ of the population size we then would have to use the fpcf to compensate, as above.)
Appendix 7  WinSample Data Directory and Technical Information

Maximum Sampling Frame Size = 1,000,000
Maximum Sample Size = 10,000
Maximum Spares = 10,000

WinSample uses the Borland Random Number Generator

Taxpayer Profile Table

File Name: Profile.DBF
COMPANY: String, 50 Positions  Company Name
USERTYPE: String, 20 Positions  Type of User
AUDITNO: String, 10 Positions  Audit Number
SAMPLES: Floating Point, 8 Positions  Total # of Samples in the Profile
COUNTER: Floating Point, 8 Positions  System Field for indexing sample files

Sample Master File (Contains the file names of all sample files in a SAM file)

File Name: SamMaster.DBF
FILENAME: String, 15 Positions  Name of Sample File
SAMPLEDESC: String, 25 Positions  Description of Sample File
SAMPLEOPT: String, 25 Positions  System Field for Sample Option
SAMPLESIZE: Floating Point, 8 Positions  Sample Size
SPARES: Floating Point, 8 Positions  # of Spares
SEED: String, 15 Positions  Seed #
POPULATION: Floating Point, 8 Positions  Population
RUNDATE: String, 20 Positions  Date the Sample was generated
Non-Statistical Sampling

### Numbered Population Sample File

File Name: Numsam.dbf
**DATAROW:** String, 1 Positions  
**System Field:**  
Y = Sample = Sample row,  
N = Range row

**BEGRANGE:** Floating Point, 8 Positions  
Beginning of Range

**ENDRANGE:** Floating Point, 8 Positions  
Ending of Range

**ORDER:** Floating Point, 8 Positions  
Order of Sample selections

**SAMPLE:** Floating Point, 8 Positions  
Sample #

**SPARES:** Floating Point, 8 Positions  
Spare #

### Time Sample File

File Name: Timsam.dbf
**DATAROW:** String, 1 Positions  
**System Field:**  
Y = Sample = Sample row,  
N = Range row

**ORDER:** Floating Point, 8 Positions  
Order of Sample selections

**PERIOD:** String, 10 Positions  
Period being sampled,  
Day, Week, Month, Quarter

**BEGPERIOD:** Date  
Beginning of Range

**ENDPERIOD:** Date  
Ending of Range

**SAMPLE:** Date  
Sample #

**SPARE:** Date  
Spare #

### Journal Sample File

File Name: Jrnsam.dbf
**DATAROW:** String, 1 Positions  
**System Field:**  
Y = Sample = Sample row,  
N = Range row

**JOURNALNO:** Floating Point, 8 Positions  
Journal # Range

**NOOFPAGES:** Floating Point, 8 Positions  
# of Pages for Journal #

**NOOFLINES:** Floating Point, 8 Positions  
# of Lines for Journal #

**ORDER:** Floating Point, 8 Positions  
Order of Sample selections

**JRNLSAMPLE:** Floating Point, 8 Positions  
Sample Journal #

**PAGESAMPLE:** Floating Point, 8 Positions  
Sample Page #

**LINESAMPLE:** Floating Point, 8 Positions  
Sample Line #

**JRNLSPARES:** Floating Point, 8 Positions  
Spare Journal #

**PAGESPARES:** Floating Point, 8 Positions  
Spare Page #

**LINESPARES:** Floating Point, 8 Positions  
Spare Line #
**Imaged Documents Sample File**

File Name: Imgsam.dbf
DATAROW: String, 1 Positions  
System Field:  
Y = Sample = Sample row,  
N = Range row

ORDER: Floating Point, 8 Positions  
Order of Sample selections
NOOFTAPES: Floating Point, 8 Positions  
Range of Tapes
NOOFFRAMES: Floating Point, 8 Positions  
Range of Frames
TAPESAMPLE: Floating Point, 8 Positions  
Sample Frame #
FRAMESAMPL: Floating Point, 8 Positions  
Sample Tape #
TAPESPARE: Floating Point, 8 Positions  
Spare Tape #
FRAMESPARE: Floating Point, 8 Positions  
Spare Frame #

**Microfiche Sample File**

File Name: Micsam16.dbf
DATAROW: String, 1 Positions  
System Field:  
Y = Sample = Sample row,  
N = Range row

ORDER: Floating Point, 8 Positions  
Order of Sample selections
MICSHEETNO: Floating Point, 8 Positions  
Range of Microfiche Sheet #s
ROWNORANGE: Floating Point, 8 Positions  
Range of Rows
COLNORANGE: Floating Point, 8 Positions  
Range of Columns
MICSAMPLE: Floating Point, 8 Positions  
Sample Microfiche Sheet #
ROWSAMPLE: Floating Point, 8 Positions  
Sample Row #
COLSAMPLE: Floating Point, 8 Positions  
Sample Column #
MICSPARE: Floating Point, 8 Positions  
Spare Microfiche Sheet #
ROWSPARE: Floating Point, 8 Positions  
Spare Row #
COLSPARE: Floating Point, 8 Positions  
Spare Column #
Appendix 8  Table Of Z Values

Appendix 9  Table Of T Values

Student’s T Distribution

W. S. Gosset at the turn of the century first studied the problem of non-normally distributed sample means for small sample sizes. The brewery at which he worked forbade his publishing anything, so he used a nom de plume “student” and used the name “t” for his random variable.

This study determined that the “student t” distribution is bell-shaped and symmetrical, much like the normal distribution. A commonly used guideline is that the “student t” distribution need only be used when the sample size is 30 or less; for larger samples, the normal distribution is ordinarily used.

The table on the next page shows the proportions of area for the t distribution. Degrees of freedom are calculated as 1 less than the sample size (n-1). The t value replaces the z value in any formulas where sample size is less than 30. For sample sizes less than 30, the sample size formula is:

\[ n = \left( \frac{t \times s}{e} \right)^2 \]

Where \( n \) = sample size  
\( t \) = value of \( t \)  
\( s \) = standard deviation  
\( e \) = acceptable magnitude for error

The formula to calculate precision (UCL = Upper Confidence Level; LCL = Lower Confidence Level) also becomes:

\[ \text{UCL} = x + (t \times s) \]
\[ \text{LCL} = x - (t \times s) \]

Where \( x \) = Sample mean  
\( t \) = value of \( t \) at the given confidence level  
\( s \) = Standard deviation of the sample
Table of T Values

![Image of t-distribution]

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Glossary

Acceptance sampling
A variant of attribute sampling.

Attribute sampling
Estimates the rate (percentage) of occurrence of a specific quality (attribute) in a population (see Appendix 5).

Average
See mean.

Central limit theorem
States that the sampling distribution of sample means approaches the normal distribution as the number of samples increases, regardless of the distribution of the population. If the central limit theorem is used, the samples drawn from the parent population must be of size 30 or more.

Confidence interval
The range of values in which the value of the population parameter of interest may be contained with the specified probability.

Confidence level
The specified probability of the confidence interval.

Mean
A measure of central tendency calculating the sum of the values in the data group divided by the number of values.

Normal deviate
The normal deviate is represented by z. A table of Z values (Appendix 8) presents the probability that the value of interest lies within a specified interval under the unit normal distribution as measured by the standard deviation.

Outliers
Items that are larger or smaller than the majority of items in the population.

Population
The entire set of values that are being audited.

Precision
The level of acceptable risk associated with using the sample mean to estimate the population mean. Also known as precision, maximum tolerable error, sampling error, and E.
Random number sampling
A table of numbers used to specifically select population elements for sample purposes.

Range
The difference between the highest and lowest values in a group of values.

Sample
A group of values selected from a population.

Sample base
The total dollar amount of all the selected sample points.

Sample point
A single record in the population selected to be audited. The sample point can be a numbered transaction, a time period (day, week, month, or quarter), a journal page and line item, an image tape and frame number, or a microfiche sheet, row, and column. Sample point can also be referred to as sample unit.

Sample unit
See sample point.

Sampling frame
A group of items from which the sample is drawn or a listing of sampling units that represents the population. It may or may not be identical to the population.

Seed Number
A randomly generated number used as a starting point for sample selection.

Simple random sample
A type of sampling in which every value in the population has an equal chance of selection for inclusion in the sample.

Spares
Extra sample points used to replace non-existent sample points or non-transactions.

Statistical sampling
Evaluating the precision of inferences about a population on the basis of information obtained from a random sample.
**Student’s t**
States that the sampling distribution of sample means approaches the normal distribution as the number of samples increases, regardless of the distribution of the population. If the student t is used, the samples drawn from the parent population must be of size 5 or more. A table of t values is in Appendix 9.

**Unit normal distribution**
A continuous probability distribution that is symmetrical. The mean, median and mode are all equal.

**Z**
See normal deviate (see Appendix 8).
Bibliography


Professional Development Institute, University of North Texas, *Statistical Sampling for State Revenue Auditors*, 2000.


